## CHEMICAL KINETICS

## Chemical Kinetics:

- The study of the Rates of Chemical Reactions: how fast do chemical reactions proceed to form products
- The study of Reaction Mechanisms: the steps involved in the change from reactants to products.


## Rates of Reactions

- Factors affecting Reaction Rates:

1. Concentration of Reactants: Rate $\alpha$ Concentration of Reactants
2. Presence of a Catalyst: A catalyst is a substance that increases the Reaction Rate without being consumed
3. Temperature: Rate $\alpha$ Temperature
4. Surface Area of Reactants: Rate $\alpha$ Surface Area of Reactants

## Definition of Reaction Reaction Rate

$$
\mathrm{H}_{2}(\mathrm{~g})+\mathrm{I}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{HI}(\mathrm{~g})
$$

Reaction Rate:
increase in the molar concentration of a product per unit time
OR
$>$ decrease in the molar concentration of reactant per unit time

$$
\text { Rate of disappearance of } \mathrm{H}_{2}=\frac{\Delta\left[\mathrm{H}_{2}\right]}{\Delta \mathrm{t}}=\frac{\text { decrease in the molar conc. of } \mathrm{H}_{2}}{\text { time interval }}
$$

- The expression above is referred to as: Average Rate over the time interval $\Delta t$

REACTION RATES


- Reactant concentration decreases with time, while product concentration increases with time.

| Time (s) | [ $\mathrm{H}_{2}$ ] (M) | $\Delta\left[\mathrm{H}_{2}\right]$ | $\Delta t$ | Rate $=-\Delta\left[\mathrm{H}_{2}\right] / \Delta t(\mathrm{M} / \mathrm{s})$ |
| :---: | :---: | :---: | :---: | :---: |
| 0.000 | 1.000 | -0.181 | 10.000 | 0.0181 |
| 10.000 | 0.819 | -0.149 | $10.000$ | $0.0149$ |
| 20.000 | 0.670 | -0.149 -0.121 | 10.000 10.000 | $0.0121$ |
| 30.000 | 0.549 | $-0.100$ | 10.000 | 0.0100 |
| 40.000 | 0.449 | $-0.081$ | 10.000 | 0.010081 |
| 50.000 | 0.368 | -0.081 | 10.000 | 0.0081 |
| 60.000 | 0.301 | -0.067 | 10.000 | 0.0067 |
| 70.000 | 0.247 | -0.054 | 10.000 | 0.0054 |
| 80.000 | 0.202 | -0.045 | 10.000 | 0.0045 |
| 90.000 | 0.165 | -0.037 | 10.000 | 0.0037 |
| 100.000 | 0.135 | -0.030 | 10.000 | 0.0030 |

## REACTION RATES

- The Reaction Rate decreases as the reaction proceeds.

Reason: the concentration of reactants decreases

- Any substance in the reaction can be used to express the Rxn. Rate

Rate of disappearance of $\mathrm{H}_{2}=\frac{\Delta\left[\mathrm{H}_{2}\right]}{\Delta \mathrm{t}}=\frac{\mathrm{H}_{2}(\mathrm{~g})+\mathrm{I}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{HI}(\mathrm{g})}{\text { decrease in the molar conc. of } \mathrm{H}_{2}}$
time interval
Rate of disappearance of $\mathrm{I}_{2}=\frac{\Delta\left[\mathrm{I}_{2}\right]}{\Delta \mathrm{t}}=\frac{\text { decrease in the molar conc. of } \mathrm{I}_{2}}{\text { time interval }}$
Rate of formation of $\mathrm{HI}=\frac{\Delta[\mathrm{HI}]}{\Delta \mathrm{t}}=\frac{\text { increase in the molar conc. of HI }}{\text { time interval }}$

- Reaction Rate is always positive
(a) Rate of formation of a product $=\frac{\Delta \text { [increase in concentration of product }]}{\Delta t}$
$\Delta$ [decrease in concentration of reactant]
(b) Rate of decomposition of a reactant $=-$
$\Delta t$

Since: $\Delta$ [decrease in concentration of reactant] has a negative value the Reaction Rate will be positive

## Reaction Rate in terms of stoichiometry

$$
\mathrm{H}_{2}(\mathrm{~g})+\mathrm{I}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{HI}(\mathrm{~g})
$$

Rate of increase of $\mathrm{HI}=2 \times$ Rate of decrease of $\mathrm{H}_{2}$

OR

$$
\frac{\text { Rate of increase of HI }}{2}
$$

Reason: 2 moles of HI are formed from reaction of 1 mole of $\mathrm{H}_{2}$

## REACTION RATES

## Examples:

1. For the hypothetical reaction shown below, write a rate expression based on each reactant and product:

$$
3 \mathrm{~A}+\mathrm{B} \rightarrow 2 \mathrm{C}+4 \mathrm{D}
$$

Rate based on $\mathrm{A}=$

$$
\text { Rate based on } \mathrm{C}=
$$

Rate based on $\mathrm{B}=$ Rate based on $\mathrm{D}=$

$$
\text { Rate }=
$$

2. Consider the following reaction:

$$
\mathrm{H}_{2} \mathrm{O}_{2}(\mathrm{aq})+3 \mathrm{I}^{-}(\mathrm{aq})+2 \mathrm{H}^{+}(\mathrm{aq}) \rightarrow \mathrm{I}_{3}^{-}(\mathrm{aq})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l})
$$

In the first 10.0 seconds of the reaction, the concentration of $\mathrm{I}^{-}$dropped from 1.000 M to 0.868 M .
a) Calculate the average rate of this reaction in this time interval.
b) Predict the rate of change in concentration of $\mathrm{H}^{+}$during this time interval.

## Examples (cont'd):

3. The following data was collected for the reaction shown below:

$$
\mathrm{C}_{4} \mathrm{H}_{8}(\mathrm{~g}) \rightarrow 2 \mathrm{C}_{2} \mathrm{H}_{4}(\mathrm{~g})
$$

a) What is the average rate of reaction between 0 and 10 seconds?

| Time (s) | $\left[\mathbf{C}_{\mathbf{4}} \mathbf{H}_{\mathbf{8}} \mathbf{( M )}\right.$ |
| :---: | :---: |
| 0 | 1.000 |
| 10 | 0.913 |
| 20 | 0.835 |
| 30 | 0.763 |
| 40 | 0.697 |
| 50 | 0.637 |

b) What is the rate of formation of $\mathrm{C}_{2} \mathrm{H}_{4}$ between 20 and 30 seconds?
4. For the reaction $A+2 B \rightarrow C$, the initial rate is $0.100 \mathrm{M} / \mathrm{s}$, at a given condition. What is $\Delta[B] / \Delta t$ under the same conditions?
a) $-0.0500 \mathrm{M} / \mathrm{s}$
b) $-0.100 \mathrm{M} / \mathrm{s}$
c) $-0.200 \mathrm{M} / \mathrm{s}$

## RATE DETERMINATION

- Rate determination is done by monitoring the change in concentration of reactant or product over time.


## Method:

- Withdraw samples from the reaction vessel at various times and analyze some of their physical or chemical properties that give information on the concentrations present.


## Properties appropriate and easy to monitor

- Color (if product or reactant absorbs light); a spectrophotometer (shown on bottom of page) can be used to quantify the difference in color difference of reactants and products.
- Volume, at constant P and T ; useful if gaseous substances are present, and \# of mol of gaseous reactants $\quad \neq \quad$ \# of mol of gaseous products
- Pressure at constant V and T; useful if gaseous substances are present, and \# of mol of gaseous reactants $\neq \quad$ \# of mol of gaseous products
- Density; useful is density of reactants $\neq$ density of products


## Properties not appropriate to monitor

- Flammability (difficult to measure quantitatively)
- Mass (mass is conserved in a chemical reaction)



## RATE LAW

- The Rate of Reaction depends on the concentration of one or more of the reactants and, for the simple reaction ( $\mathrm{A} \rightarrow$ products) it can be written as:

$$
\text { Rate }=k[A]^{\mathrm{n}}
$$

- The relationship above is called the Rate Law, where $\boldsymbol{k}$ is a constant of proportionality called the rate constant and $\boldsymbol{n}$ is the reaction order. This relationship describes how the rate of a reaction changes with respect to the concentration of a reactant.
- For a more general reaction with general equation of the form:

$$
\mathbf{a A}+\mathbf{b B} \xrightarrow{\mathbf{c}} \mathbf{d D}+\mathbf{e E}
$$

the Rate Law has the form: $\quad$ Rate $=k[A]^{m}[B]^{n}[C]^{p}$
where,

| $\mathbf{m}, \mathbf{n}$, and $\mathbf{p}$ | $>$ are reaction orders with respect to each reactant or the catalyst, |
| ---: | :--- |
|  | $>$ are frequently, but not always integers |
|  | $>$ are determined experimentally |
|  | are $\underline{\text { not the coefficients in the balanced chemical equation }}$ |

and

$$
\begin{array}{ll}
\mathbf{k} & >\text { is the Rate Constant } \\
> & \text { with its units depending upon the form of Rate Law } \\
> & \text { and its value depending on temperature }
\end{array}
$$

## REACTION ORDER

- Reaction Order is the exponent ( $n$ ) of the concentration of that species in the Rate Law, as determined experimentally.
- When $\mathrm{n}=0$, the reaction is zero order, when $\mathrm{n}=1$, the reaction is first order and when $\mathrm{n}=2$, the reaction is second order.
- Although other orders are possible, including fractional or negative orders, they are not common.


## Zero-Order Reaction:

- In a zero-order reaction, the rate of the reaction is independent of the reactant concentration.

$$
\text { Rate }=\mathrm{k}[\mathrm{~A}]^{0}=\mathrm{k}
$$

- Zero-order reactions occur under conditions where the actual amount of reactant available for a reaction does not change as the overall amount of reactant changes.
- For example, sublimation is usually zero order, since the amount of substance on the surface available to sublime does not change as the substance sublimes.


## First-Order Reaction:



- In a first-order reaction, the rate of a reaction is directly proportional to the concentration of the reactant.

$$
\text { Rate }=\mathrm{k}[\mathrm{~A}]^{1}
$$

- Therefore, the rate of a first-order reaction slows down as the reaction proceeds because the concentration of the reactant decreases.
- Furthermore, the rate of the reaction increases with the same change factor in concentration of the reactant. For example, doubling the concentration of a reactant in a first-order reaction, doubles the rate of reaction.


## Second-Order Reaction:

- In a second-order reaction, the rate of a reaction is proportional to square of the concentration of the reactant.

$$
\text { Rate }=\mathrm{k}[\mathrm{~A}]^{2}
$$

- Therefore, the rate of a second-order reaction is more sensitive to the concentration of the reactant. Furthermore, since the rate of the reactant increases with the square of the change factor in concentration of the reactant, doubling the concentration of a reactant in a second-order reaction, quadruples the rate of reaction.


## REACTION ORDER

- Effect of concentration change on reaction rates and orders can be summarized as:

| Order | Effect of Doubling <br> Concentration | Rate |
| :---: | :---: | :---: |
| Zero | $2^{0}$ | No Effect |
| First | $2^{1}$ | $\mathbf{x} 2$ |
| Second | $2^{2}$ | $\mathbf{x 4}$ |
| Negative | $2^{-1}$ | $\mathbf{x}^{1 / 2}$ |
| Half | $2^{1 / 2}$ | $\sqrt{2}$ |

- Diagram A below shows how the concentration of reactant changes with time for the three common reaction orders, with identical rate constant $(\mathrm{k})$ and initial concentrations.
- Diagram B shows how the rate of reaction changes as a function of reactant concentration.



## EXPERIMENTAL DETERMINATION OF RATE LAW

- In determining the rate law for a reaction, first the order of reaction with respect to each reactant and catalyst must be found.
- Commonly a series of experiments are done in which the initial concentrations of reactants are varied (usually doubled).
- The results of these experiments will yield the respective orders of reaction.

Example:

$$
2 \mathrm{~N}_{2} \mathrm{O}_{5}(\mathrm{~g}) \longrightarrow 4 \mathrm{NO}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})
$$

|  | Initial $\mathbf{N}_{\mathbf{2}} \mathbf{O}_{5}$ Conc. <br> $(\mathbf{M})$ | Initial Rate of Disappearance <br> of $\mathbf{N}_{\mathbf{2}} \mathbf{O}_{\mathbf{5}}(\mathbf{M} / \mathbf{s})$ |
| :--- | :---: | :---: |
| Experiment 1 | $1.0 \times 10^{-2}$ | $4.8 \times 10^{-6}$ |
| Experiment 2 | $2.0 \times 10^{-2}$ | $9.6 \times 10^{-6}$ |

Rate $=\mathbf{k}\left[\mathrm{N}_{2} \mathrm{O}_{5}\right]^{\mathrm{m}} \quad \mathrm{m}=$ ? (must be determined from experimental data)

$$
\frac{\text { Rate Exp. } 2}{\text { Rate Exp. } 1}=\frac{\mathrm{k}(2)^{\mathrm{m}}}{\mathrm{k}(1)^{\mathrm{m}}}=\frac{9.6 \times 10^{-6}}{4.8 \times 10^{-6}}=2
$$

$\begin{array}{ll}\text { Experimental: } & >\text { Doubling }\left[\mathrm{N}_{2} \mathrm{O}_{5}\right] \text { doubled the rate of reaction } \\ \text { It follows: } & >\mathrm{m}=1\left(2^{1}=2\right) \\ \text { The Reaction is: } & >\text { First order in } \mathrm{N}_{2} \mathrm{O}_{5} \\ & >\text { First order overall }\end{array}$

$$
\text { Rate }=\mathbf{k}\left[\mathbf{N}_{2} \mathrm{O}_{5}\right]^{1} \quad \text { Rate }=\mathbf{k}\left[\mathbf{N}_{2} \mathrm{O}_{5}\right]
$$

## Examples:

1. Use the rate data below to
A) determine the reaction orders with respect to $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right],\left[\mathrm{I}^{-}\right]$and $\left[\mathrm{H}^{+}\right]$and
B) find the rate constant k for the reaction shown below:

$$
\mathrm{H}_{2} \mathrm{O}_{2}(\mathrm{aq})+3 \mathrm{I}^{-}(\mathrm{aq})+2 \mathrm{H}^{+}(\mathrm{aq}) \longrightarrow \mathrm{I}_{3}^{-}(\mathrm{aq})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l})
$$

|  | Initial Concentrations $(\mathbf{M})$ |  |  | Initial Rate <br> $\mathbf{n}$ <br>  <br>  <br> $\mathbf{M} / \mathbf{s})$ |
| :---: | :---: | :---: | :---: | :---: |
| Experiment 1 | 0.010 | $\left[\mathbf{H}_{2}\right]$ | 0.010 |  |
| $\left.\mathbf{I}^{-}\right]$ | 0.00050 | $2.3 \times 10^{-6}$ |  |  |
| Experiment 2 | 0.020 | 0.010 | 0.00050 | $2.30 \times 10^{-6}$ |
| Experiment 3 | 0.010 | 0.020 | 0.00100 | $1.15 \times 10^{-6}$ |
| Experiment 4 | 0.010 | 0.010 |  |  |

## Solution

A) Compare two rate experiments in which all concentrations of reactants but one are held constant:
[ $\mathrm{H}_{2} \mathrm{O}_{2}$ ] : Compare Experiment 1 and Experiment 2 When [ $\mathrm{H}_{2} \mathrm{O}_{2}$ ] is doubled, the Rate is doubled It follows: $2^{\mathrm{m}}=2$
$\mathrm{m}=1$ 1st order in $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]$
[ $\left.I^{-}\right]$: $\quad$ Compare Experiment 1 and Experiment 3 When [ $I^{-}$] is doubled, the Rate is doubled It follows: $2^{n}=2$
$\mathrm{n}=1$ 1st order in [ $\left.\mathbf{I}^{-}\right]$
$\left[\mathrm{H}^{+}\right]: \quad$ Compare Experiment 1 and Experiment 4 When $\left[\mathrm{H}^{+}\right]$is doubled, the Rate does not change It follows: $2^{\mathrm{p}}=1 \quad \mathrm{p}=0 \quad \mathbf{0}$ order in $\left[\mathrm{H}^{+}\right]$

$$
\mathrm{H}_{2} \mathrm{O}_{2}(\mathrm{aq})+3 \mathrm{I}^{-}(\mathrm{aq})+2 \mathrm{H}^{+}(\mathrm{aq}) \longrightarrow \mathrm{I}_{3}^{-}(\mathrm{aq})+2 \mathrm{H}_{2} \mathrm{O}(\mathrm{l})
$$

Summary: 1 st order in $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]$
1st order in $\quad\left[\mathrm{I}^{-}\right]$
0 order in $\left[\mathrm{H}^{+}\right]$

$$
\text { RATE }=\mathrm{k}\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]^{1}\left[\mathrm{I}^{-}\right]^{1}\left[\mathrm{H}^{+}\right]^{0}
$$

commonly written :

$$
\mathrm{RATE}=\mathrm{k}\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]\left[\mathrm{I}^{-}\right]
$$

NOTE: Reaction Orders are not related to the coefficients of the overall equation

## Examples (cont'd):

B) Find the Rate Constant, k

From Experiment 1: (any other experiment could be used)
$\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]=0.010 \mathrm{M}$
$\left[\mathrm{I}^{-}\right]=0.010 \mathrm{M}$
Rate $=1.15 \times 10^{-6} \mathrm{M} / \mathrm{s}$
$\mathrm{k}=$ ?

RATE $=k\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]\left[\mathrm{I}^{-}\right]$

$$
\mathrm{k}=\frac{\text { Rate }}{\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]\left[\mathrm{I}^{-}\right]}=\frac{1.15 \times 10^{-6} \mathrm{M} / \mathrm{s}}{(0.010 \mathrm{M})(0.010 \mathrm{M})}=1.2 \times 10^{-2} \mathrm{M}^{-1} \mathrm{~s}^{-1}
$$

2. Use the rate data below to
A) determine the rate law for the reaction $\mathrm{A}+\mathrm{B} \rightarrow \mathrm{C}$, and
B) calculate the rate constant k , and
C) calculate the rate of reaction for experiment 4

| Experiment <br> Number | $[\mathbf{A}]$ <br> $\mathbf{( M )}$ | $[\mathbf{B}]$ <br> $(\mathbf{M})$ | Initial Rate <br> $(\mathbf{M} / \mathbf{s})$ |
| :---: | :---: | :---: | :---: |
| 1 | 0.100 | 0.100 | $4.0 \times 10^{-5}$ |
| 2 | 0.100 | 0.200 | $4.0 \times 10^{-5}$ |
| 3 | 0.200 | 0.100 | $16.0 \times 10^{-5}$ |
| 4 | 0.050 | 0.100 | $? ? ? ?$ |

## Examples (cont'd):

1. The reaction below was experimentally determined to be $1^{\text {st }}$ order with respect to $\mathrm{O}_{2}$ and $2^{\text {nd }}$ order with respect to NO. Which mixture in the diagram below has the fastest initial rate?

2. The graph below shows a plot of the rate of reaction versus the concentration of the reactant A for the reaction $\mathrm{A} \rightarrow$ products.
a. What is the order of the reaction with respect to A ?
b. Write the rate law for the reaction and determine the value of $k$.


## INTEGRATED RATE LAW (1 ${ }^{\text {ST }}$ ORDER REACTION)

- The rate laws discussed earlier examine the relationship between concentration of a reactant and the rate of a reaction. But often, the relationship between the concentration of a reactant and time is of interest.
- The integrated rate law for a reaction is a relationship between the concentrations of the reactants and time. For example, consider a simple first order decomposition reaction shown below:

$$
\mathrm{A} \longrightarrow \text { products }
$$

$$
\text { Rate Law: } \quad \text { Rate }=k[A]
$$

- Since Rate $=-\Delta[\mathrm{A}] / \Delta \mathrm{t}$, the following can be written:


## Differential Rate Law

$$
-\frac{\Delta[\mathrm{A}]}{\Delta \mathrm{t}}=\mathrm{k}[\mathrm{~A}]
$$

- Calculus can be used to integrate the differential rate law and obtain the $1^{\text {st }}$ order integrated rate law:


## Integrated Rate Law

$$
\ln \frac{[\mathrm{A}]_{\mathrm{t}}}{[\mathrm{~A}]_{0}}=-k t
$$

- The integrated rate law can be used to calculate the concentration of reactant at any time during the reaction.


## Examples:

1. Sulfuryl chloride, $\mathrm{SO}_{2} \mathrm{Cl}_{2}$, decomposes when heated:

$$
\mathrm{SO}_{2} \mathrm{Cl}_{2}(\mathrm{~g}) \quad \longrightarrow \mathrm{SO}_{2}(\mathrm{~g}) \quad+\quad \mathrm{Cl}_{2}(\mathrm{~g})
$$

In an experiment, the initial concentration of $\mathrm{SO}_{2} \mathrm{Cl}_{2}$ was 0.0248 M . If the reaction is first order with the Rate Constant of $2.2 \times 10^{-5} \mathrm{~s}^{-1}$, what is the concentration of $\mathrm{SO}_{2} \mathrm{Cl}_{2}$ after 2.5 hours?

$$
\begin{array}{rl}
{[\mathrm{A}]_{0}=0.0248 \mathrm{M}} & \mathrm{k}=2.2 \times 10^{-5} \mathrm{~s}^{-1} \quad \mathrm{t}=2.5 \mathrm{~h}(9 \underline{0} 00 \mathrm{~s}) \\
\ln \frac{[\mathrm{A}]_{\mathrm{t}}}{[\mathrm{~A}]_{0}}=-\mathrm{kt} & \ln \frac{[\mathrm{~A}]_{\mathrm{t}}}{0.0248}=-\left(2.2 \times 10^{-5} \mathrm{~s}^{-1}\right)(9 \underline{0} 00 \mathrm{~s})=-0.1 \underline{9} 8
\end{array}
$$

Taking antilog of both sides,

$$
\frac{[\mathrm{A}]_{\mathrm{t}}}{0.0248}=\mathrm{e}^{-0.198}=0.82 \quad[\mathrm{~A}] \mathrm{t}=(0.0248)(0.82)=2.0 \times 10^{-2} \mathrm{M}
$$

## Examples (cont'd):

2. Cyclobutane, $\mathrm{C}_{4} \mathrm{H}_{8}$ decomposes, when heated to give ethylene:

$$
\mathrm{C}_{4} \mathrm{H}_{8}(\mathrm{~g}) \longrightarrow 2 \mathrm{C}_{2} \mathrm{H}_{4}(\mathrm{~g})
$$

The reaction is first order. In an experiment, the initial $\left[\mathrm{C}_{4} \mathrm{H}_{8}\right]=0.00150 \mathrm{M}$.
After heating at $450^{\circ} \mathrm{C}$ for 455 seconds, $\left[\mathrm{C}_{4} \mathrm{H}_{8}\right]=0.00119 \mathrm{M}$. Based on this information, determine the rate constant for this reaction at this temperature.

$$
\begin{array}{r}
{\left[\mathrm{C}_{4} \mathrm{H}_{8}\right]_{0}=0.00150 \mathrm{M} \quad\left[\mathrm{C}_{4} \mathrm{H}_{8}\right]_{455}=0.00119 \mathrm{M}} \\
\ln \frac{\left[\mathrm{C}_{4} \mathrm{H}_{8}\right]_{455}}{\left[\mathrm{C}_{4} \mathrm{H}_{8}\right]_{0}}=\ln \frac{0.00119 \mathrm{M}}{0.00150 \mathrm{M}}=-\mathrm{k}(455 \mathrm{~s})
\end{array}
$$

$$
\ln 0.79 \underline{3} 3=-455 \mathrm{k}
$$

$$
-0.23 \underline{16}=-455 k
$$

$$
\mathrm{k}=5.09 \times 10^{-4} \mathrm{~s}^{-1}
$$

3. Cyclopropane rearranges to form propene in the gas phase:


The reaction is first order and has a rate constant of $3.36 \times 10^{-5} \mathrm{~s}^{-1}$ at 720 K . If the initial concentration of cyclopropane is 0.0445 M , what will the cyclopropane concentration be after 235.0 min ?

## HALF-LIFE ( $\mathbf{t}_{1 / 2}$ ) OF A FIRST ORDER REACTION

- Half-life is the time it takes for the reactant concentration to decrease to one-half of its initial value.

$$
\ln \frac{[\mathrm{A}]_{\mathrm{t}}}{[\mathrm{~A}]_{0}}=-\mathrm{kt}
$$

In one half-life $\left(\mathrm{t}_{1 / 2}\right): \quad[\mathrm{A}]_{\mathrm{t}}=\frac{1}{2}[\mathrm{~A}]_{0} \quad \Longleftrightarrow \ln \frac{\frac{1}{2}[\mathrm{~A}]_{0}}{[\mathrm{~A}]_{0}}=-\mathrm{k}\left(\mathrm{t}_{1 / 2}\right)$

$$
-0.693=-\mathrm{k}\left(\mathrm{t}_{1 / 2}\right) \quad \longleftrightarrow \quad \mathbf{t}_{1 / 2}=\frac{\mathbf{0 . 6 9 3}}{\mathbf{k}}
$$

## NOTES:

$\Rightarrow$ Half-Life does not depend on the initial concentration, $[\mathrm{A}]_{0}$
Half-Life for a First-Order Reaction

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## Example:

1. Dinitrogen pentoxide, decomposes when heated in carbon tetrachloride solvent:

$$
\mathrm{N}_{2} \mathrm{O}_{5}(\mathrm{~g}) \longrightarrow 2 \mathrm{NO}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g})
$$

The rate law is first order in $\mathrm{N}_{2} \mathrm{O}_{5}$ with a rate constant of $6.2 \times 10^{-4} \mathrm{~min}^{-1}$. What is the half-life for this reaction?

$$
\mathrm{t}_{1 / 2}=\frac{0.693}{\mathrm{k}}=\frac{0.693}{6.2 \times 10^{-4} \mathrm{~min}^{-1}}=1118 \mathrm{~min}=1.1 \times 10^{3} \mathrm{~min}
$$

2. A first order reaction has a half-life of 26.4 seconds. How long does it take for the concentration of the reactant to fall to $1 / 8$ of its initial value?
3. The radioactive decay of $\mathrm{U}-238$ is first order with a half-life of $4.5 \times 10^{9}$ years. How long would it take for $10 \%$ of the U-238 atoms in a sample to U-238 to decay?

## GRAPHING FIRST ORDER REACTIONS

- The order of a reaction can be determined by graphing the experimental data. For a first order reaction, the integrated rate law can be written as:
- First order Rate Law:
$\ln \frac{[\mathrm{A}]_{t}}{[\mathrm{~A}]_{0}}=-\mathrm{kt}$
- This equation may be rewritten:

$$
\left.\ln [\mathrm{A}]_{\mathrm{t}}=-\mathrm{kt}+\ln [\mathrm{A}]_{0} \quad \text { (This is the equation of a straight line, } \mathrm{y}=\mathrm{mx}+\mathrm{b}\right)
$$

- A plot of $\ln [A](y)$ versus time $(\boldsymbol{x})$ should give a straight line for a first order reaction with a slope of $-\boldsymbol{k}$ and a y-intercept of $\ln [\boldsymbol{A}] 0$.
- For example, for the decomposition of $\mathrm{SO}_{2} \mathrm{Cl}_{2}$ (shown below), the concentration vs. time data can be graphed to show that the reaction is first order.



## GRAPHING FIRST ORDER REACTIONS

## Example:

1. Use the graph provided on the previous page to determine the concentration of $\mathrm{SO}_{2} \mathrm{Cl}_{2}$ at 1900 s . (Round to 3 significant figures)
2. Shown below is a graph of concentration vs. time for decomposition of $\mathrm{CH}_{3} \mathrm{CN}$. Determine the order of the reaction and the value of rate constant at this temperature.


## INTEGRATED RATE LAW ( $\mathbf{2}^{\text {ND }}$ ORDER REACTION)

$\mathrm{a} \mathrm{A} \longrightarrow$ Products

Rate $=-\frac{\Delta[\mathrm{A}]}{\Delta \mathrm{t}}=\mathrm{k}[\mathrm{A}]^{2} \longleftarrow \quad$ Differential Rate Law
By using calculus:

$$
\frac{1}{[\mathrm{~A}]_{\mathrm{t}}}=\mathrm{kt}+\frac{1}{[\mathrm{~A}]_{0}} \longleftarrow \quad \text { Integrated Rate Law }
$$

## Example:

1. For the reaction

$$
2 \mathrm{NO}_{2}(\mathrm{~g}) \longrightarrow 2 \mathrm{NO}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})
$$

At 330 K :

$$
\begin{aligned}
& \mathrm{k}=0.775 \mathrm{M}^{-1} \mathrm{~s}^{-1} \quad[\mathrm{~A}]_{0}=0.0030 \mathrm{M} \\
& \frac{1}{[\mathrm{~A}]_{\mathrm{t}}}=\left(0.775 \mathrm{M}^{-1} \mathrm{~s}^{-1}\right)(645 \mathrm{~s})+\frac{1}{0.0030 \mathrm{M}} \\
& \frac{1}{[\mathrm{~A}]_{\mathrm{t}}}=(4945=? \\
& {[\mathrm{A}]_{\mathrm{t}}=\mathbf{0 . 0 0 1 2} \mathbf{~ M}}
\end{aligned}
$$

## HALF-LIFE ( $\mathbf{t}_{1 / 2}$ ) OF A $2^{\text {ND }}$ ORDER REACTION

- Half-life is the time it takes for the reactant concentration to decrease to one-half of its initial value.

For a second order reaction: $\quad$ Rate $=k[A]^{2} \quad$ and $\frac{1}{[\mathrm{~A}]_{\mathrm{t}}}=\mathrm{kt}+\frac{1}{[\mathrm{~A}]_{0}}$
In one half-life $\left(\mathrm{t}_{1 / 2}\right): \quad[\mathrm{A}]_{\mathrm{t}}=\frac{1}{2}[\mathrm{~A}]_{0} \quad \rightleftharpoons \quad \frac{1}{0.5[\mathrm{~A}]_{0}}=\mathrm{kt}+\frac{1}{[\mathrm{~A}]_{0}}$

$$
\mathrm{kt}_{1 / 2}=\frac{1}{0.5[\mathrm{~A}]_{0}}-\frac{1}{[\mathrm{~A}]_{0}}=\frac{1}{[\mathrm{~A}]_{0}}
$$



## NOTES:

$\triangleright$ Half-Life depends on the initial concentration, $[\mathrm{A}]_{0}$
$\triangleright$ Half-Life increases as reaction progresses

## Example:

1. For a particular $2^{\text {nd }}$ order reaction $\mathrm{k}=0.775 \mathrm{M}^{-1} \mathrm{~s}^{-1}$.
a) How long does it take to the concentration to decrease from 0.0030 M to 0.0015 ?

For concentration to drop to half of its original value, $t=$ half-life

$$
\mathrm{t}_{1 / 2}=\frac{1}{\mathrm{k}[\mathrm{~A}]_{0}}=\frac{1}{\left(0.775 \mathrm{M}^{-1} \mathrm{~s}^{-1}\right)(0.0030 \mathrm{M})}=430 \mathrm{~s}
$$

b) How long does it take for the concentration to be halved again?

$$
\mathrm{t}_{1 / 2}=\frac{1}{\mathrm{k}[\mathrm{~A}]_{0}}=\frac{1}{\left(0.775 \mathrm{M}^{-1} \mathrm{~s}^{-1}\right)(0.0015 \mathrm{M})}=860 \mathrm{~s} \quad \longleftarrow \quad \text { Twice as long }
$$

## GRAPHING $2^{\text {ND }}$ ORDER REACTIONS

- The second order integrated rate law is in the form of a an equation for a straight line.

$$
\begin{aligned}
\frac{1}{[\mathbf{A}]_{\mathrm{t}}} & =\mathbf{k} \mathbf{t}+\frac{1}{[\mathbf{A}]_{0}} \\
\mathbf{y} & =\mathbf{m} \mathbf{x}+\mathbf{b}
\end{aligned}
$$

- A plot of $\mathbf{1 / [ A ] _ { t }}(\mathbf{y})$ versus time (s) should give a straight line for a second order reaction with a slope of $\mathbf{k}$ and y -intercept of $\mathbf{1 / [ A ] 0 .}$


Summary:
To determine the order of a reaction,

1. Collect time vs. concentration data for the reaction.
2. Assuming $1^{\text {st }}$ order, plot $\ln [\mathrm{A}]$ vs. time.
3. If a linear graph is obtained, then it is $1^{\text {st }}$ order.
4. If no linear graph, then plot $1 /[\mathrm{A}]$ vs. time.
5. If a linear graph is obtained, then it is $2^{\text {nd }}$ order.

## Example:

1. Given the experimental data listed on the right, determine if the reaction shown below is $1^{\text {st }}$ or $2^{\text {nd }}$ order, and determine the rate constant $(\mathrm{k})$ for the reaction shown below:

$$
\mathrm{NO}_{2}(\mathrm{~g}) \longrightarrow \mathrm{NO}(\mathrm{~g})+\mathrm{O}(\mathrm{~g})
$$

## Strategy:

> We must first see if the data fits the Rate Law for $1^{\text {st }}$ Order Reactions. If it does, the reaction is of the $1^{\text {st }}$ order
$>$ If it does not, we must see if the data fits the Rate Law for $2^{\text {nd }}$ Order If it does, the reaction is of the $2^{\text {nd }}$ order

First Order Rate Law:

$$
\ln [\mathbf{A}]_{\mathrm{t}}=-\mathbf{k} \mathbf{t}+\ln [\mathbf{A}]_{0}
$$

$$
\mathbf{y}=\mathbf{m} \mathbf{x}+\mathbf{b}
$$

Plot $\ln [A]_{t}$ as a function of $t$

## Second order Rate Law



Plot $1 /[\mathrm{A}]_{\mathrm{t}}$ as a function of t

| Time (s) | [ $\mathrm{NO}_{2}$ ] (M) |
| :---: | :---: |
| 0 | 0.01000 |
| $50$ | 0.00887 |
| $100$ | $0.00797$ |
| $150$ | 0.00723 |
| $200$ | $0.00662$ |
| $250$ | $0.00611$ |
| $300$ | $0.00567$ |
| $350$ | $0.00528$ |
| $400$ | $0.00495$ |
| $450$ | $0.00466$ |
| $500$ | $0.00440$ |
| $550$ | $0.00416$ |
| $600$ | $0.00395$ |
| $650$ | $0.00376$ |
| $700$ | $0.00359$ |
| $750$ | $0.00343$ |
| $800$ | $0.00329$ |
| $850$ | $0.00316$ |
| $900$ | $0.00303$ |
| $950$ | $0.00292$ |
| 1000 | 0.00282 |


> Not a straight line
$>$ Reaction is not of $1^{\text {st }}$ Order


$>$ A straight line is obtained
$>\quad$ Reaction is of $\mathbf{2}^{\text {nd }}$ Order

$$
\mathrm{k}=\text { slope }=0.255 \mathrm{M}^{-1} \mathrm{~s}^{-1}
$$

## SUMMARY OF KINETICS EQUATIONS

| Order | Rate <br> Law | Units of $k$ | Integrated <br> Rate Law | Straight-Line Plot | Half-Life <br> Expression |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | Rate $=k[\mathrm{~A}]^{0}$ | $\mathrm{M} \cdot \mathrm{s}^{-1}$ | $[\mathrm{A}]_{\mathrm{t}}=-k t+[\mathrm{A}]_{0}$ |  | $t_{1 / 2}=\frac{[A]_{0}}{2 k}=\frac{1}{k} \frac{[A]_{0}}{2}$ |
| 1 | Rate $=k[A]^{\text {l }}$ | $s^{-1}$ | $\ln [A]_{t}=-k t+\ln [A]_{0}$ $\ln \frac{[A]_{t}}{[A]_{0}}=-k t$ |  | $t_{1 / 2}=\frac{0.693}{k}=\frac{1}{k}(0.693)$ |
| 2 | Rate $=k[A]^{2}$ | $\mathrm{M}^{-1} \cdot \mathrm{~s}^{-1}$ | $\frac{1}{[\mathrm{~A}]_{t}}=k t+\frac{1}{[\mathrm{~A}]_{0}}$ |  | $t_{1 / 2}=\frac{1}{k[A]_{0}}=\frac{1}{k} \frac{1}{[A]_{0}}$ |

## Examples:

1. The data shown below was collected for the reaction:

$$
\mathrm{CH}_{3} \mathrm{Cl}(\mathrm{~g})+3 \mathrm{Cl}_{2}(\mathrm{~g}) \longrightarrow \mathrm{CCl}_{4}(\mathrm{~g})+3 \mathrm{HCl}(\mathrm{~g})
$$

| $\left[\mathbf{C H}_{\mathbf{3}} \mathbf{C l}\right] \mathbf{( M )}$ | $\left[\mathbf{C l}_{\mathbf{2}}\right] \mathbf{( M )}$ | Initial Rate $(\mathbf{M} / \mathbf{s})$ |
| :---: | :---: | :---: |
| 0.050 | 0.050 | 0.014 |
| 0.100 | 0.050 | 0.029 |
| 0.100 | 0.100 | 0.041 |
| 0.200 | 0.200 | 0.115 |

Write the rate law and calculate the rate constant for this reaction.

$$
\begin{aligned}
& \text { Rate }= \\
& \mathrm{k}=
\end{aligned}
$$

## Examples (cont'd):

2. The reaction shown below is found to be first order with respect to A , second order with respect to B and zero order with respect to C . Answer the following questions based on this information.

$$
\mathrm{A}+\mathrm{B}+\mathrm{C} \rightarrow \text { product }
$$

a) Write a rate law for this reaction.
b) By what factor does the reaction rate change if the concentrations of all the three reactants double?
c) By what factor does the reaction rate change if the concentration of A is doubled and concentration of B is halved?
3. In a kinetic study of the reaction shown below, the following data were obtained for the initial rates of disappearance of A and B

$$
\mathrm{A}+2 \mathrm{~B} \longrightarrow \mathrm{C}
$$

| Exp. | $[\mathbf{A}]$ <br> $\mathbf{( M )}$ | $[\mathbf{B}]$ <br> $\mathbf{( M )}$ | Initial Rate <br> $(\mathbf{M} / \mathbf{s})$ |
| :---: | :---: | :---: | :---: |
| 1 | 0.010 | 0.010 | $1.5 \times 10^{-6}$ |
| 2 | 0.030 | 0.010 | $4.5 \times 10^{-6}$ |
| 3 | 0.020 | 0.020 | $1.2 \times 10^{-5}$ |

Write the rate law and calculate the rate constant for this reaction.

$$
\begin{aligned}
& \text { Rate = } \\
& \mathrm{k}=
\end{aligned}
$$

4. In the presence of excess thiocyanate ion $\left(\mathrm{SCN}^{-}\right)$the following reaction is 1 st order with respect to $\mathrm{Fe}^{3+}$ with a rate constant of $1.27 \mathrm{~s}^{-1}$.

$$
\mathrm{Fe}^{3+}(\mathrm{aq})+\mathrm{SCN}^{-}(\mathrm{aq}) \longrightarrow \mathrm{Fe}(\mathrm{SCN})^{2+}(\mathrm{aq})
$$

a) What is the Half-Life in seconds?

$$
t_{1 / 2}=
$$

b) How many seconds would be required for the initial concentration of $\mathrm{Fe}^{3+}$ to decrease to each of the following values? ( $25.0 \%$ and $12.5 \%$ )
c) How many seconds are required for $90.0 \%$ of reaction to be completed?
5. The graph below was prepared for the reaction:
AB (g) $\qquad$ $A(g)+B(g)$
a) Determine the order of the reaction and the value of the rate constant.
b) Predict the concentration of AB at 25 seconds.

c) Determine the rate of the reaction when the concentration of AB is 0.10 M ?

## TEMPERATURE AND RATE

- The rate of reaction depends on temperature, and the rate law for a reaction can be expressed as:

$$
\text { Rate }=k[A]^{\mathrm{n}}
$$

- The temperature dependence of the rate is contained in the rate constant $(k)$, which is a constant only when the temperature remains constant.
- An increase in temperature generally results in an increase in k , which results in a faster rate. This relationship is expressed in the Arrhenius equation, which relates the rate constant $(\mathrm{k})$ to the temperature in Kelvin.

- In this equation,
$>\mathbf{R}=$ gas constant $(8.314 \mathrm{~J} / \mathrm{molK})$
$>\mathbf{E}_{\mathbf{a}}=$ Activation energy (energy barrier)
$>\mathbf{A}=$ frequency factor (the number of times reactants approach the activation barrier per unit time)

To better understand these factors, we examine the reaction in which $\mathrm{CH}_{3} \mathrm{NC}$ (methyl isonitrile) rearranges to form $\mathrm{CH}_{3} \mathrm{CN}$ (acetonitrile):


## TEMPERATURE AND RATE

## Activation Energy:

- Activation energy $\left(\mathrm{E}_{\mathrm{a}}\right)$ is defined as the energy barrier that must be overcome for reactants to transform into products.
- To get from reactants to products, the molecule must go through a high energy intermediate state called the activated complex or transition state.

- For transformation of $\mathrm{CH}_{3} \mathrm{NC}$ to $\mathrm{CH}_{3} \mathrm{CN}$, even though the overall reaction is energetically downhill (exothermic), it must first go uphill (endothermic) to reach the activated complex, because energy is required to initially weaken the $\mathrm{H}_{3} \mathrm{C}-\mathrm{N}$ bond to allow rotation.

Bond weakens


NC group begins to rotate

## Frequency Factor:

- For this reaction, the frequency factor represents each time the NC part of the molecule begins to rotate (wags) and approaches the activation barrier.
- Note that approaching the activation barrier is not equivalent to overcoming the barrier. Most of the approaches do not have enough energy to overcome the barrier.

Each wag is an approach to the activation barrier.

Reaction progress

## TEMPERATURE AND RATE

## Exponential Factor:

- The exponential factor is a number between 0 and 1 that represents the fraction of molecules that possess enough energy to overcome the activation barrier. The exponential factor is the fraction of approaches that are actually successful and result in the product.
- The exponential factor depends on both the temperature $(T)$ and the activation energy $\left(\mathrm{E}_{\mathrm{a}}\right)$ of the reaction:

$$
\text { Exponential factor }=\mathrm{e}^{-\mathrm{E}_{\mathrm{a}} / R T}
$$

- A low activation energy and a high temperature make the negative exponent small, so the exponential factor approaches 1. A high activation energy and a low temperature make the exponent a very large negative number, so the exponential factor becomes small.
- The effect of increase in temperature on the energy of the particles is shown in the diagram below. As the temperature increases, the fraction of molecules with enough energy to surmount the activation energy increases.



## Summarizing Temperature and Reaction Rates:

$>$ The frequency factor is the number of times the reactants approach the activation barrier per unit time.
$>$ The exponential factor is the fraction of approaches that are successful in surmounting the activation barrier and forming products.
> The exponential factor increases with increasing temperature but decreases with increasing activation energy.

## ARRHENIUS PLOTS: DETERMINATION OF A \& E $\mathbf{a}_{\mathbf{a}}$

- The frequency factor $(A)$ and the activation energy $\left(\mathrm{E}_{\mathrm{a}}\right)$ are important quantities in understanding the kinetics of any reaction. These factors can be measured in the laboratory by manipulating and rearranging the Arrhenius equation as shown below:

$$
\mathrm{k}=\mathrm{A} \mathrm{e}^{-\mathrm{E}_{\mathrm{a}} / R T}
$$

- Taking natural log of both sides of the equation above,

$$
\begin{aligned}
& \ln \mathrm{k}=\ln \left(\mathrm{Ae}^{-\mathrm{E}_{\mathrm{a}} / \mathrm{RT}}\right) \\
& \ln \mathrm{k}=\ln \mathrm{A}-\frac{\mathrm{E}_{\mathrm{a}}}{\mathrm{RT}}
\end{aligned}
$$

- Rearranging the last equation above we can obtain:

$$
\ln k=-\frac{E_{a}}{R}\left(\frac{1}{T}\right)+\ln A
$$

- The equation above is in the form of a straight line. A plot of $\boldsymbol{l n} \boldsymbol{k}$ vs $\mathbf{1 / T}$ (in Kelvin) results a straight line with slope equal to $-\boldsymbol{E}_{a} / \boldsymbol{R}$. Such plot is called the Arrhenius plot and is commonly used in the analysis of kinetic data.


## Examples:

1. The kinetic data, shown below, was collected for the decomposition of ozone. Determine the frequency factor and the activation energy (in $\mathrm{kJ} / \mathrm{mol}$ ) for this reaction.

$$
\mathrm{O}_{3}(\mathrm{~g}) \rightarrow \mathrm{O}_{2}(\mathrm{~g})+\mathrm{O}(\mathrm{~g})
$$

| Temperature ( K ) | Rate Constant ( $\mathbf{M}^{\mathbf{- 1}} \cdot \mathrm{s}^{\mathbf{- 1}}$ ) | Temperature ( K ) | Rate Constant ( $\mathbf{M}^{\mathbf{- 1}} \cdot \mathbf{s}^{\mathbf{- 1}}$ ) |
| :---: | :---: | :---: | :---: |
| 600 | $3.37 \times 10^{3}$ | 1300 | $7.83 \times 10^{7}$ |
| 700 | $4.85 \times 10^{4}$ | 1400 | $1.45 \times 10^{8}$ |
| 800 | $3.58 \times 10^{5}$ | 1500 | $2.46 \times 10^{8}$ |
| 900 | $1.70 \times 10^{6}$ | 1600 | $3.93 \times 10^{8}$ |
| 1000 | $5.90 \times 10^{6}$ | 1700 | $5.93 \times 10^{8}$ |
| 1100 | $1.63 \times 10^{7}$ | 1800 | $8.55 \times 10^{8}$ |
| 1200 | $3.81 \times 10^{7}$ | 1900 | $1.19 \times 10^{9}$ |

## Examples (cont'd):

To determine A and $\mathrm{E}_{\mathrm{a}}$, a plot of $\ln \mathrm{k}$ vs $1 / \mathrm{T}$ is prepared, using the data above.


Activation energy can be calculated from the slope:

$$
\begin{aligned}
& \mathrm{m}=\frac{-\mathrm{E}_{\mathrm{a}}}{\mathrm{R}}=-1.12 \times 10^{4} \mathrm{~K} \\
& \mathrm{E}_{\mathrm{a}}=-\left(-1.12 \times 10^{4} \mathrm{~K}\right)(8.314 \mathrm{~J} / \mathrm{molK})=9.31 \times 10^{4} \mathrm{~J} / \mathrm{mol}=93.1 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

The frequency factor can be determined from the y-intercept:

$$
\ln \mathrm{A}=26.8
$$

$$
\mathrm{A}=\mathrm{e}^{26.8}=4.36 \times 10^{11}
$$

2. Use the results obtained in problem above to determine the rate constant at 298 K for the decomposition of ozone.

## Examples (cont'd):

3. Reaction A and reaction B have identical frequency factors. However, reaction B has a higher activation energy than reaction A . Which reaction has a greater rate constant at room temperature?
4. Use the Arrhenius plot shown below to determine the frequency factor $(A)$ and activation energy $\left(E_{a}\right.$, in $\mathrm{kJ} / \mathrm{mol}$ ) for the first order decomposition of $\mathrm{N}_{2} \mathrm{O}$ :

$$
\mathrm{N}_{2} \mathrm{O}(\mathrm{~g}) \rightarrow \mathrm{N}_{2}(\mathrm{~g})+\mathrm{O}(\mathrm{~g})
$$



## COLLISION THEORY

- Earlier we discussed the frequency factor as representing the number of approaches to the activation barrier per unit time. Let's now apply this to a reaction involving two gas-phase reactants:

$$
\mathrm{A}(\mathrm{~g})+\mathrm{B}(\mathrm{~g}) \rightarrow \text { products }
$$

- Based on collision theory, a chemical reaction occurs after a sufficiently energetic collision between two reactant molecules.
- Furthermore, collision theory separates the frequency factor (A) into two distinct parts, as shown in the equations below:

- The collision frequency $(\mathrm{z})$ is the number of collisions that occur per unit time, which can be calculated from the pressure of the gases and the reaction temperature. The orientation factor (p) represents the fraction of the collisions with orientation that allows the reaction to occur.
- The orientation factor can be better understood by considering the reaction shown below:

- In order for the above reaction to occur, two molecules of sufficient energy and proper orientation must collide. Therefore, as shown below, not all collisions of sufficient energy will lead to products, since they do not possess proper orientation.

- Some reactions have orientation factors that are much smaller than one. This indicates that the orientation requirements for these reactions are very stringent, and molecules must be aligned in a very specific way for the reaction to occur. One such example is shown below:

$$
\mathrm{H}_{2}(\mathrm{~g})+\mathrm{CH}_{2}=\mathrm{CH}_{2}(\mathrm{~g}) \rightarrow \mathrm{CH}_{3}-\mathrm{CH}_{3}(\mathrm{~g}) \quad \mathrm{p}=1.7 \times 10^{-6}
$$

- Reactions between atoms usually have orientation factors of approximately 1 because atoms are spherical and thus any orientation will lead to the formation of product.


## Examples:

1. Which reaction below would you expect to have the smallest orientation factor? Explain.
a) $\mathrm{H}(\mathrm{g})+\mathrm{I}(\mathrm{g}) \rightarrow \mathrm{HI}(\mathrm{g})$
b) $\mathrm{H}_{2}(\mathrm{~g})+\mathrm{I}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{HI}(\mathrm{g})$
c) $\mathrm{HCl}(\mathrm{g})+\mathrm{HCl}(\mathrm{g}) \rightarrow \mathrm{H}_{2}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g})$
2. 

## POTENTIAL - ENERGY DIAGRAMS FOR REACTIONS

- A potential energy diagram shows how the energy of the reactants, activated complex and products are related for an endothermic and for an exothermic reaction.


## Endothermic Reactions



## Exothermic Reactions

(activated complex)


## Examples:

1. The diagram below shows the energy of a reaction as the reaction progresses. Label each blank box in the diagram.

2. Sketch a potential energy diagram for the decomposition of nitrous oxide:

$$
2 \mathrm{~N}_{2} \mathrm{O}(\mathrm{~g}) \rightarrow 2 \mathrm{~N}_{2}(\mathrm{~g})+\mathrm{O}_{2}(\mathrm{~g})
$$

The activation energy for the forward reaction is 251 kJ ; the $\Delta \mathrm{H}^{\circ}$ is +167 kJ . What is the activation energy for the reverse reaction? Label the diagram appropriately.

## REACTION MECHANISMS

- Reaction Mechanisms show the steps involved in the change from Reactants to Products
- Mechanisms consist of a set of "Elementary Reactions" whose overall effect is the Net Chemical Equation.


## Elementary Reactions:

- Elementary reactions are single molecular events that result in a reaction and are caused by molecular collisions

$$
\mathrm{NO}_{2}(\mathrm{~g})+\mathrm{CO}(\mathrm{~g}) \longrightarrow \mathrm{NO}(\mathrm{~g})+\mathrm{CO}_{2}(\mathrm{~g}) \quad \text { Net Chemical Equation }
$$

Below 500 K , this reaction takes place in 2 steps:
Elementary Reaction 1: $\quad \mathrm{NO}_{2}+\mathrm{NO}_{2} \xrightarrow[\substack{\text { Reaction } \\ \text { intermediate } \\ \text { (short-lived) }}]{\mathrm{NO}_{3}}+\mathrm{NO}$

Elementary Reaction 2: $\mathrm{NO}_{3}+\mathrm{CO} \longrightarrow \mathrm{NO}_{2}+\mathrm{CO}_{2}$

- Adding the steps (Elementary Reactions) yields the Overall Equation:

$$
\begin{aligned}
& \mathrm{NO}_{2}+\mathrm{NO}_{2} \longrightarrow \mathrm{NO}_{3}+\mathrm{NO} \\
& \mathrm{NO}_{3}+\mathrm{CO} \longrightarrow \mathrm{NO}_{2}+\mathrm{CO}_{2} \\
& \mathrm{NO}_{2}+\mathrm{CO} \longrightarrow \mathrm{NO}+\mathrm{CO}_{2} \quad \text { Overall Equation }
\end{aligned}
$$

## Examples:

1. The decomposition of Ozone $\left(\mathrm{O}_{3}\right)$ is believed to occur in 2 steps:

| Elementary Reaction 1: | $\mathrm{O}_{3}$ | $\rightleftarrows \mathrm{O}_{2}$ | + |  |
| :--- | :--- | :--- | :--- | :--- |
| Elementary Reaction 2: | $\mathrm{O}_{3}$ | + | O | $\longrightarrow 2 \mathrm{O}_{2}$ |

Identify any Reaction Intermediate:
What is the Overall equation?

## Examples (cont'd):

2. Sodium hydrogen carbonate ( $\mathbf{N a H C O}_{3}$ ), also called sodium bicarbonate can been synthesized through a sequence of 3 elementary steps:

| $\mathrm{CO}_{2} \mathrm{~g}$ ) | + | $\mathrm{H}_{2}$ | $\longrightarrow$ | $\mathrm{H}_{2} \mathrm{CO}_{3}$ ( |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{CO}_{3}(\mathrm{aq})$ | + | $\mathrm{NH}_{4} \mathrm{OH}$ |  | $\mathrm{NH}_{4} \mathrm{HCO}_{3}(2$ |
| $\mathrm{NH}_{4} \mathrm{HCO}_{3}(\mathrm{aq})+\mathrm{NaCl}(\mathrm{aq})$ |  |  |  | $\mathrm{HCO}_{3}(\mathrm{~s})+$ |

Identify the Reaction Intermediates:

Write the Overall Equation:


## MOLECULARITY

- Molecularity is the number of molecules on the reactant side of an Elementary Reaction.


## Unimolecular Reactions:

- Unimolecular reactions are Elementary Reactions that involve one reactant molecule.
- These are commonly the decomposition reactions of unstable species.

$$
\underset{\substack{\text { excited } \\ \text { molecule }}}{\mathrm{O}_{3}{ }^{*} \longrightarrow \mathrm{O}_{2}}+{ }^{+}
$$

## Bimolecular Reactions:

- Bimolecular reactions are Elementary Reactions that involve two reactant molecules.
- These are very common reactions.

$$
\mathrm{O}=\mathrm{N}+\mathrm{Cl}-\mathrm{Cl} \longrightarrow \mathrm{O}=\mathrm{N}-\mathrm{Cl} \quad+\mathrm{Cl}
$$

## Termolecular Reactions:

- Termolecular reactions are Elementary Reactions that involve three reactant molecules.
- These are less common because the chance of three molecules coming together with the right orientation is unlikely.


## Examples:

1. What is the molecularity of each of the following elementary reactions?
$\mathrm{O}+\mathrm{O}_{2}+\mathrm{N}_{2} \longrightarrow \mathrm{O}_{3}+\mathrm{N}_{2}{ }^{*}$
$\mathrm{NO}_{2} \mathrm{Cl}+\mathrm{Cl} \longrightarrow \mathrm{NO}_{2}+\mathrm{Cl}_{2}$
$\mathrm{Cl}+\mathrm{H}_{2} \longrightarrow \mathrm{HCl}+\mathrm{H}$
$\mathrm{CS}_{2} \longrightarrow \mathrm{CS}+\mathrm{S}$

## Rate Equation for an Elementary Reaction

I. For an Overall Reaction, the Rate Law cannot be predicted by the Overall Equation

## Reasons:

- The majority of reactions consist of several elementary steps.
- The Rate Law is the combined result of the elementary steps
- The rate of all the elementary reactions must be known in order to predict the rate law for the overall equation.
II. For an Elementary Reaction, the Rate Law can be written directly from the Elementary Equations
- The rate of an elementary reaction is proportional to the product of the concentrations of each reactant molecule.

1. Unimolecular Elementary Reactions
$\mathrm{A} \longrightarrow$
B +
C

$$
\text { Rate }=\mathrm{k}[\mathrm{~A}]
$$

2. Bimolecular Elementary Reactions

$$
\mathrm{A}+\mathrm{B} \longrightarrow \mathrm{C}+\mathrm{D} \quad \text { Rate }=\mathrm{k}[\mathrm{~A}][\mathrm{B}]
$$

Reason:

- The frequency of collisions is proportional to the number of A molecules $\left(\mathrm{n}_{\mathrm{A}}\right)$ and the number of B molecules ( $\mathrm{n}_{\mathrm{B}}$ )


## 3. Termolecular Elementary Reactions

$$
\mathrm{A}+\mathrm{B}+\mathrm{C} \longrightarrow \mathrm{D}+\mathrm{E} \quad \text { Rate }=\mathrm{k}[\mathrm{~A}][\mathrm{B}][\mathrm{C}]
$$

## Examples:

Write Rate Equations for each of the elementary reactions shown below:

1) $\mathrm{O}_{3}+\mathrm{NO} \longrightarrow \mathrm{O}_{2}+\quad \mathrm{NO}_{2}$

Rate $=$
2)
$\mathrm{CS}_{2} \longrightarrow \mathrm{CS}+\mathrm{S}$
Rate $=$
3)
$2 \mathrm{NO}_{2} \longrightarrow \mathrm{~N}_{2} \mathrm{O}_{4}$

Rate $=$

## NOTE:

- For elementary reactions ONLY, the coefficients of the balanced chemical elementary reaction are the exponents to which the concentrations of the reactants are raised.


## THE RATE LAW AND THE MECHANISM

- The Suggested Mechanism for a particular reaction:
$>$ cannot be observed directly,
$>$ is a rationalized explanation based on experimental data,
$>$ is accepted provisionally, and may be replaced by another suggested mechanism based on further experimentation.
- A Suggested Mechanism
$>$ Is considered correct if it agrees with the experimentally determined Rate Law

Is considered incorrect if it does not agree with the experimentally determined Rate Law

## Example 1:

Overall Equation:

$$
2 \mathrm{NO}_{2}(\mathrm{~g})+\mathrm{F}_{2}(\mathrm{~g}) \longrightarrow 2 \mathrm{NO}_{2} \mathrm{~F}(\mathrm{~g})
$$

Experimental Rate Law: $\quad$ Rate $=\mathrm{k}\left[\mathrm{NO}_{2}\right]\left[\mathrm{F}_{2}\right]$
NOTE: $1^{\text {st }}$ order with respect to $\mathrm{NO}_{2}$
$1^{\text {st }}$ order with respect to $\mathrm{F}_{2}$
$2^{\text {nd }}$ order Overall

## Predicted Possible Mechanisms:

1. One Single Elementary Reaction
$\mathrm{NO}_{2}+\mathrm{NO}_{2}+\mathrm{F}_{2} \longrightarrow 2 \mathrm{NO}_{2} \mathrm{~F} \quad$ (Termolecular)
Predicted Rate Law: Rate: $\mathrm{k}\left[\mathrm{NO}_{2}\right]^{2}\left[\mathrm{~F}_{2}\right]$
NOTE: $2^{\text {nd }}$ order with respect to $\mathrm{NO}_{2}$
$1^{\text {st }}$ order with respect to $\mathrm{F}_{2}$
$3^{\text {rd }}$ order overall

- The predicted Rate Law does not agree with the experimental Rate Law
- This mechanism must be incorrect.

2. Two Single Elementary Reactions

|  | $\mathrm{NO}_{2}$ | $+\mathrm{F}_{2}$ | $\xrightarrow{\mathrm{k}_{1}} \mathrm{NO}_{2} \mathrm{~F}+\mathrm{F}$ |
| :--- | :--- | :--- | :--- |
|  | $\mathrm{NO}_{2}$ | +F | (slow step) |
| Overall: | $2 \mathrm{NO}_{2}+\mathrm{F}_{2} \longrightarrow \mathrm{NO}_{2} \mathrm{~F}$ | (fast step) |  |
| $2 \mathrm{NO}_{2} \mathrm{~F}$ |  |  |  |

Reaction Intermediate: F

## NOTE:

$>$ The Rate Law is determined by the slow step
THE SLOWEST STEP $\longrightarrow$ THE RATE DETERMINING STEP
$>$ Predicted Rate Law $=$ RATE (rate-determining-step) $=\mathrm{k}_{1}\left[\mathrm{NO}_{2}\right]\left[\mathrm{F}_{2}\right]$

$$
\begin{array}{ll}
\text { NOTE: } & 1^{\text {st }} \text { order with respect to } \mathrm{NO}_{2} \\
& 1^{\text {st }} \text { order with respect to } \mathrm{F}_{2} \\
& 2^{\text {nd }} \text { order overall }
\end{array}
$$

- The predicted Rate Law agrees with the experimental Rate Law
- This mechanism must be correct.

| Predicted Rate Law |  |
| :--- | :--- |
| Rate $=\mathrm{k}_{1}\left[\mathrm{NO}_{2}\right]\left[\mathrm{F}_{2}\right]$ | $\frac{\text { Experimental Rate Law }}{\text { Rate }=\mathrm{k}\left[\mathrm{NO}_{2}\right]\left[\mathrm{F}_{2}\right]}$ |

The two Rate Laws are identical if: $\mathrm{k}_{1}=\mathrm{k}$

## Example 2:

The following mechanism has been proposed for decomposition of ozone to oxygen gas:

$$
\begin{aligned}
& \mathrm{O}_{3} \stackrel{\mathrm{k}_{1}}{\rightleftarrows} \mathrm{O}_{2}+\mathrm{O} \quad \text { (fast equilibrium) } \\
& \mathrm{O}_{3}+\mathrm{O} \xrightarrow{\mathrm{k}_{2}} 2 \mathrm{O}_{2}
\end{aligned}
$$

Determine the Rate Law based on this mechanism.

## CATALYSIS

- Earlier we learned that reaction rates can be increased by various factors, such as increasing concentration or increasing temperature. But sometimes these methods are not feasible. Alternately, reaction rates can also be increased by use of a catalyst.
- A catalyst is a substance that speeds up a reaction without being consumed. In theory the catalyst may be used over and over again. In practice, however, there is some loss of catalyst through other reactions that occur at the same time (side-reactions).
- A catalyst works by providing an alternate mechanism for the reaction-one in which the ratedetermining step has a lower activation energy. For example, consider the noncatalytic destruction of ozone in the upper atmosphere:

$$
\mathrm{O}_{3}(\mathrm{~g})+\mathrm{O}(\mathrm{~g}) \longrightarrow 2 \mathrm{O}_{2}(\mathrm{~g})
$$

Energy Diagram for Catalyzed and Uncatalyzed Pathways
 energy than the uncatalyzed pathway, it occurs at a much faster rate.

- Although the reaction described above is an undesirable use of a catalyst, many catalysts are used to speed up desirable reactions. For example, the catalytic converter in your car is used to convert harmful exhaust pollutants such as nitrogen monoxide and carbon monoxide into less harmful substances:

$$
2 \mathrm{NO}(\mathrm{~g})+2 \mathrm{CO}(\mathrm{~g}) \xrightarrow{\text { catalyst }} \mathrm{N}_{2}(\mathrm{~g})+2 \mathrm{CO}_{2}(\mathrm{~g})
$$

- The catalytic converter also promotes the complete combustion of any fuel fragments present in the exhaust, preventing potential formation of air pollutants in the atmosphere.



## HOMOGENEOUS \& HETEROGENEOUS CATALYSIS

- Catalysts can be categorized into two types: homogeneous and heterogeneous.
- In homogeneous catalysis the catalyst exists in the same phase (state) as the reactants. The catalyzed destruction of ozone by Cl is an example of this type of catalysis.
- In heterogeneous catalysis the catalyst exists in a different phase than the reactants. The solid catalysts used in the automobile catalytic converters is an example of this type of catalysis.

- Another example of heterogeneous catalysis is the hydrogenation of double bonds in alkenes. For example, the reaction between ethene and hydrogen is a relatively slow reaction at normal temperatures:

$$
\mathrm{H}_{2} \mathrm{C}=\mathrm{CH}_{2}(\mathrm{~g})+\mathrm{H}_{2}(\mathrm{~g}) \longrightarrow \mathrm{H}_{3} \mathrm{C}-\mathrm{CH}_{3}(\mathrm{~g})
$$

- However, in presence of a catalyst, the reaction occurs rapidly. The catalysis occurs by the fourstep process shown below.
- The large activation energy of the hydrogenation reaction-due primarily to the strength of the hydrogen-hydrogen bond in $\mathrm{H}_{2}$ - is greatly lowered when the reactants adsorb onto the surface of the catalyst.



## ENZYME CATALYSIS

- Enzymes are the catalysts of biological organisms.
- Enzymes are large protein molecules that are highly specific sites in their structure, called active sites. The properties and shape of the active site is just right to bind the reactant molecule, called the substrate.
- The general mechanism by which an enzyme (E) binds a substrate (S) and then reacts to form the products $(\mathrm{P})$ is:

$$
\begin{array}{ll}
\mathrm{E}+\mathrm{S} \rightleftharpoons \mathrm{ES} & \text { Fast } \\
\mathrm{ES} \longrightarrow \mathrm{E}+\mathrm{P} & \text { Slow, rate determining }
\end{array}
$$

Enzyme-Substrate Binding


- Breakdown of sucrose (table sugar) into glucose and fructose in the body, a slow reaction at normal body temperatures, is facilitated by the catalysis with the enzyme sucrase.



## Answers to In-Chapter Problems:

| Page | Example <br> No. | Answer |
| :---: | :---: | :---: |
| 4 | 1 | $\text { Rate }=-\frac{1}{3} \frac{\Delta[\mathrm{~A}]}{\Delta \mathrm{t}}=-\frac{\Delta[\mathrm{B}]}{\Delta \mathrm{t}}=\frac{1}{2} \frac{\Delta[\mathrm{C}]}{\Delta \mathrm{t}}=\frac{1}{4} \frac{\Delta[\mathrm{D}]}{\Delta \mathrm{t}}$ |
|  | 2 | a) $4.40 \times 10^{-3} \mathrm{M} / \mathrm{s} \quad$ b) $-8.80 \times 10^{-3} \mathrm{M} / \mathrm{s}$ |
| 5 | 4 | $8.7 \times 10^{-3} \mathrm{M} / \mathrm{s} \quad$ b) $1.4 \times 10^{-2} \mathrm{M} / \mathrm{s}$ |
|  | 5 | c |
| 12 | 2A | Rate $=\mathrm{k}[\mathrm{A}]^{2}$ |
|  | 2B | $\mathrm{k}=4.0 \times 10^{-3} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ |
|  | 2C | Rate (4) $=1.0 \times 10^{-5} \mathrm{M} / \mathrm{s}$ |
| 13 | 3 | c |
|  | 4 | a) First order $\quad$ b) $\mathrm{k}=0.010 \mathrm{~s}^{-1}$ |
| 15 | 3 | 0.0277 M |
| 17 | 2 | 79.2 s |
|  | 3 | $6.8 \times 10^{8} \mathrm{yrs}$ |
| 19 | 1 | $5.78 \times 10^{-2} \mathrm{M}$ |
|  | 2 | $1{ }^{\text {st }}$ order $\quad \mathrm{k}=0.0461 \mathrm{hr}^{-1}$ |
| 24 | 1 | Rate $=\mathrm{k}\left[\mathrm{CH}_{3} \mathrm{Cl}\right]\left[\mathrm{Cl}_{2}\right]^{1 / 2} \quad \mathrm{k}=1.3 \mathrm{M}^{-1 / 2} \mathrm{~s}^{-1}$ |
| 25 | 2 | a) $\begin{array}{lll}\text { Rate }=\mathrm{k}[\mathrm{A}][\mathrm{B}]^{2} & \text { b) } 8 & \text { c) } 1 / 2\end{array}$ |
|  | 3 | Rate $=\mathrm{k}[\mathrm{A}][\mathrm{B}]^{2} ; \mathrm{k}=1.5 \mathrm{M}^{-2} \mathrm{~s}^{-1}$ |
| 26 | 4 | a) $\mathrm{t}_{1 / 2}=0.546 \mathrm{~s}$ <br> b) $\mathrm{t}=1.09 \mathrm{~s}(25 \%) ; 1.64 \mathrm{~s}(12.5 \%)$ <br> c) $\mathrm{t}=1.81 \mathrm{~s}$ |
|  | 5 | a) $2^{\text {nd }}$ order; $\mathrm{k}=2.25 \times 10^{-2} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ <br> b) $[\mathrm{AB}]=0.617 \mathrm{M}$ <br> c) $2.25 \times 10^{-4} \mathrm{M} / \mathrm{s}$ |
| 31 | 2 | $2.09 \times 10^{-5} \mathrm{M}^{-1} \mathrm{~s}^{-1}$ |
| 32 | 3 | Reaction A is faster and therefore has a larger rate constant |
|  | 4 | $\mathrm{E}_{\mathrm{a}}=251 \mathrm{~kJ} / \mathrm{mol} \quad \mathrm{A}=7.93 \times 10^{11}$ |
| 34 | 1 | c |
| 36 | 2 | $\mathrm{E}_{\mathrm{a}}($ reverse rxn) $=84 \mathrm{~kJ}$ |

